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Deep Audio Redundancy (DRED) Extension for the Opus Codec  
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## Abstract

This document proposes a mechanism for embedding very low bitrate deep audio redundancy (DRED) within the Opus codec (RFC6716) bitstream.

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## 1. Introduction

This document proposes a mechanism for embedding very low bitrate deep audio redundancy (DRED) within the Opus codec [RFC6716] bitstream.

## 1.1. Requirements Language

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in BCP 14 [RFC2119] [RFC8174] when, and only when, they appear in all capitals, as shown here.

## 2. DRED Description

Opus already includes a low-bitrate redundancy (LBRR) mechanism to transmit redundancy in-band to improve robustness to packet loss. LBRR is however limited to a single frame of redundancy, and typically uses about 2/3 of the bitrate of the "regular" Opus packet. The DRED extension allows up to one second or more redundancy to be included in each packet, using a bitrate about 1/50 of the regular

Opus bitrate. Although the amount of redundancy that can be encoded in a packet is unbounded, there appears to be little use to including more than a few seconds.

DRED is transmitted within the Opus padding, as described in [opus-extension]. In the case of multi-frame packets, there SHOULD only be one DRED extension per packet and it SHOULD be associated with the first frame of the packet. In all cases, there MUST NOT be more than one DRED extension associated to the same frame.

The DRED encoder SHOULD remove any leading or trailing silence from the redundant audio data. That being said, silence that occurs between speech segments cannot be left out. Any Selective Forwarding Unit (SFU) designed not to forward silent packets SHOULD still forward DRED-containing packets from the last known active source. Conference mixers SHOULD either forward DRED from the last known active source or re-encode DRED from the mixed audio.

DRED works by having the encoder transmit acoustic features in the Opus bitstream. On the receiver side, if packets are lost, then the first packet to arrive will contain the acoustic features for a certain duration in the past. The decoder can then use the features to synthesize the missing speech -- either from the last received or from the last audio samples produced by packet loss concealment (PLC). Although the synthesized speech samples should be consistent with the last known samples at the point of the transition, the features do not contain waveform-specific or phase-specific information so the synthesized speech waveform will significantly deviate from the original waveform, despite sounding similar.

## 2.1. Acoustic Features

DRED uses 20 acoustic features to synthesize speech. The first 18 are Bark-frequency cepstral coefficients (BFCC) and the last represent the pitch frequency and the voicing information. The BFCC features are based on bands that match the CELT bands, as shown in Table 1.

| Band | Start frequency (Hz) | Center frequency (Hz) | End frequency (Hz) |
|------|----------------------|-----------------------|--------------------|
| 0    | 0                    | 0                     | 200                |
| 1    | 0                    | 200                   | 400                |
| 2    | 200                  | 400                   | 600                |
| 3    | 400                  | 600                   | 800                |
| 4    | 600                  | 800                   | 1000               |
| 5    | 800                  | 1000                  | 1200               |
| 6    | 1000                 | 1200                  | 1400               |
| 7    | 1200                 | 1400                  | 1600               |
| 8    | 1400                 | 1600                  | 2000               |
| 9    | 1600                 | 2000                  | 2400               |
| 10   | 2000                 | 2400                  | 2800               |
| 11   | 2400                 | 2800                  | 3200               |
| 12   | 2800                 | 3200                  | 4000               |
| 13   | 3200                 | 4000                  | 4800               |
| 14   | 4000                 | 4800                  | 5600               |
| 15   | 4800                 | 5600                  | 6800               |
| 16   | 5600                 | 6800                  | 8000               |
| 17   | 6800                 | 8000                  | 8000               |

Table 1: Band definitions for DRED

TODO: Specify exact computation of the cepstral features and voicing.  
 Open question: how do we specify the neural pitch estimator?

## 2.2. Rate-Distortion-Optimized Variational Autoencoder (RDO)

The features described above need to be transmitted to the decoder with the fewest number of bits possible. Although it is not acceptable to make redundancy from one packet depend on the redundancy of another packet, we can use as much prediction as we like within one packet. In practical use, the same audio feature vector is included in many different packets (50 for 1 second redundancy). For that reason, we do not want to fully re-encode acoustic features for each packet. On the decoder side, since the most recent audio is the most likely to be used, we minimize the computation time by having the audio encoded from the most recent, going backward in time.

TODO: Specify the cepstral features and voicing. Open question: how do we specify the neural pitch estimator?

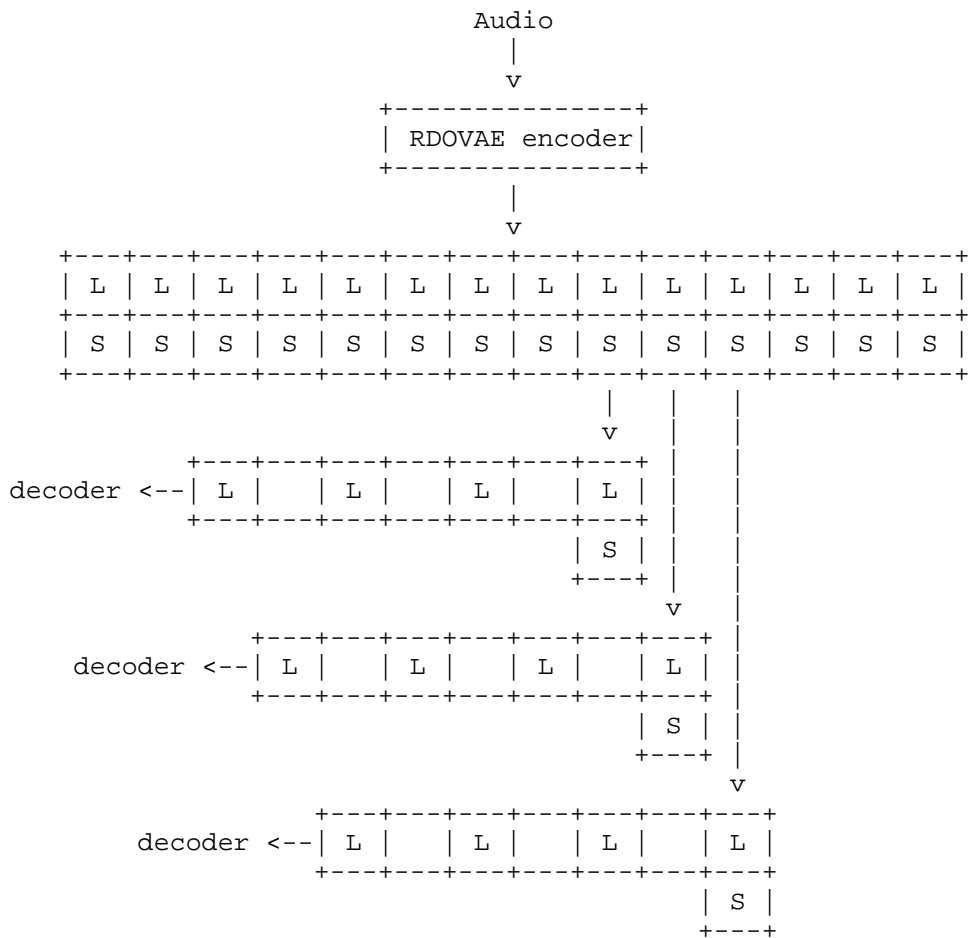


Figure 1: DRED encoding/decoding

### 2.2.1. Encoder architecture

Every 20 ms, the encoder takes in a pair of 20-dimensional acoustic feature vectors as input and produces one initial state (IS) and one latent vector. Each latent vector encodes 40 ms (their information overlaps), so only half the latent vectors need to be transmitted. Although an encoder is provided for reference, the encoder architecture is not normative. Each redundancy packet contains the latest initial state, along with latent vectors ordered from the latest (the one aligned with the initial state) to the earliest one the encoder includes. Each component of the IS and latent vectors are quantized and then entropy-coded following a Laplace distribution. The same procedure is used for both the latent vectors

and the initial state (we will describe the process for a latent variable). The quantized index  $X$  is obtained by scaling the  $i$ 'th latent variable  $z_i$  by a scaling factor  $s_{\{i,q\}}$  that depends on both  $i$  and on the quantizer  $q$ . We then apply a "dead-zone" function  $\text{zeta}(z) = z - d \cdot \tanh(z / (d + \epsilon))$ , where  $d$  also depends on  $i$  and  $q$ , and  $\epsilon = 0.1$ . The result is then rounded to the nearest integer:  $X = \text{round}(\text{zeta}(s_{\{i,q\}} * z_i))$ . The Laplace distribution used for entropy coding is parameterized with a probability that the value is zero ( $p_0$ ), as well as a decay factor  $r$  ( $0 < r < 1$ ). Both  $p_0$  and  $r$  depend on  $i$  and  $q$ . The probability  $p(X)$  for a coefficient is given by:

$$P(X) = \begin{cases} p_0 & , \quad \text{if } X = 0 \\ \frac{(1 - p_0) * r^{|X|}}{2 * (1 - r)} & , \quad \text{if } X \neq 0 \end{cases}$$

#### 2.2.2. Decoder architecture

Unlike the encoder, the decoder is normative. The decoder uses the same Laplace distribution above to decode the symbols and then scales them back by  $1/s_{\{i,q\}}$ . The initial state is used as input to initialize the decoder's gated recurrent units (GRUs). The latent vectors are used one at a time as input the DNN decoder, which produces 4 vectors of 20 acoustic features for each input latent vector.

The decoder is mostly structured as a DenseNet network, with 5 sets of alternating GRU and convolutional layers. Let `gru1..gru5` denote the 5 GRUs, `conv1..conv5` denote the 5 convolutional layers, `hidden_init/gru_init/densel/output` denote fully-connected layers, `glu1..glu5` denote gated linear units (GLUs), and `cat()` denote tensor concatenation. All GRU layers have 96 outputs (number of neurons) and all convolutional layers have 32 outputs. Despite using a functional notation, both the GRU and convolutional layers have an internal state when used one latent vector at a time. The fully-connected layers all have different sizes. Unless otherwise noted, the GRUs, convolutional and fully-connected layers all use  $\tanh$  output activations and the GRUs use sigmoid as gate activation. GLUs are defined as:

$$L(y) = \text{sigmoid}(W * y) * y$$

where  $y$  is the input and  $W$  is a square matrix of the same dimensions as  $y$ . The decoder starts with the 18-dimensional initial state vector  $IS$ . The  $IS$  is used to compute the GRU initialization vector  $V$  using both `hidden_init` and `gru_init`:

```
V = gru_init(hidden_init(IS))
```

where `hidden_init` has 18 inputs and 128 output, and `D2` has 128 inputs and 480 ( $5 \times 96$ ) outputs. The components of  $V$  are split (sequentially) into the  $V1..V5$  initialization vectors (original state before the decoding process) for GRUs `gru1..gru5`. Let  $Z$  be the decoded 20-dimensional latent vector for a particular 40-ms chunk. From there, the DenseNet structure can be expressed as:

```
t1 = densel(Z)
t2 = cat(t1, conv1(t1))
t3 = cat(t2, glu1(gru1(t2)))
t4 = cat(t3, conv2(t3))
t5 = cat(t4, glu2(gru2(t4)))
t6 = cat(t5, conv3(t5))
t7 = cat(t6, glu3(gru3(t6)))
t8 = cat(t7, conv4(t7))
t9 = cat(t8, glu4(gru4(t8)))
t10 = cat(t9, conv5(t9))
t11 = cat(t10, glu5(gru5(t10)))
x = output(t11)
```

where  $t1..tN$  are temporary vectors and "output" is the only layer to have a linear output activation, with 80 output neurons ( $4 \times 20$ ). The dimensionality of  $t1..t11$  (and corresponding GRU/convolutional input size) can be inferred from the concatenation operations. The output vector  $x$  is split (sequentially) into 4 feature vectors of 20 dimensions each that can be sent to the vocoder as packets are lost.

#### 2.2.2.1. Decoder weights

The decoder weights are distributed outside of this document at <https://media.xiph.org/opus/ietf/draft-ietf-mlcodec-opus-dred-01-weights.bin>. [FIXME: Find permanent location for the weights] They are distributed in a simple binary format that can also be used to separate them from an implementation binary for easier downloads. Each weight matrix is stored separately as a single array block. Each block starts with a 64-byte header, followed by a multiple of 64 bytes of array data. Blocks are self-delimited and can be concatenated into a single file.



The header starts with a 4-byte Header ID representing the string "DNNw", followed by a 4-byte Version number (currently 0). The Type of the weights follows, encoded as a 4-byte integer, where value 0 represents floating point weights and value 3 represents 8-bit signed integers. The 4-byte Size field that follows represents the size of the data in bytes (not number of elements), and the Block Size is the number of data bytes rounded up to 64 bytes. The block size indicates where the next block is expected. Note that the block size does not include the header size. The remaining 44 bytes of the header contain the name of the array.

For implementation efficiency, the binary format can be implemented using any endianness, but for the purpose of distributing the reference weights, we use a little-endian format.

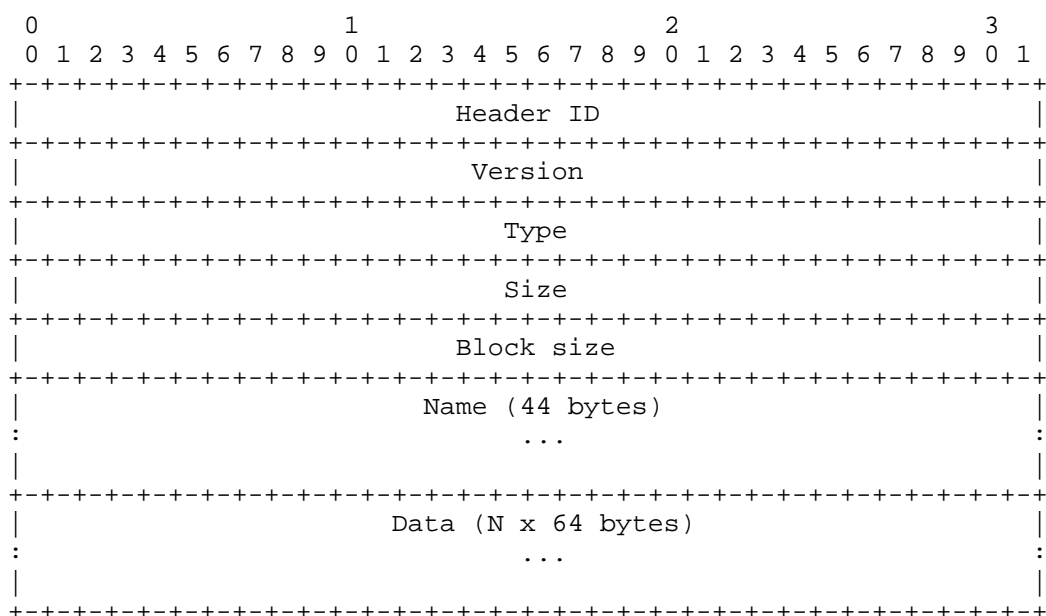


Figure 2: Binary Weights Format

The decoder arrays are named `dec_<layer name>_<variable name>`, where the names are `gru1..gru5`, `con1..conv5`, and so on. There is an optional `_float` or `_int8` suffix for type when relevant. Variable names can be "bias", "subbias", "scale" and "weights". TODO: more on how the matrices are used.

### 2.2.3. Statistical data

We define 16 different quantization settings, ranging from  $q=0$  (higher bitrate) to  $q=15$  (lower bitrate). For each quantizer and for each latent variable or initial state coefficient, we have a normative scale ( $s$ ), decay ( $r$ ), and  $p_0$  value. Note that the dead-zone parameters  $d$  are not normative.

| k  | Q0  | Q1  | Q2  | Q3  | Q4  | Q5  | Q6  | Q7 | Q8 | Q9 | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |
|----|-----|-----|-----|-----|-----|-----|-----|----|----|----|-----|-----|-----|-----|-----|-----|
| 0  | 255 | 208 | 168 | 134 | 106 | 82  | 64  | 48 | 36 | 26 | 17  | 10  | 3   | 3   | 2   | 2   |
| 1  | 255 | 219 | 187 | 160 | 137 | 117 | 101 | 81 | 70 | 50 | 23  | 6   | 6   | 5   | 3   | 2   |
| 2  | 255 | 218 | 187 | 160 | 138 | 118 | 102 | 84 | 71 | 63 | 31  | 7   | 7   | 5   | 3   | 2   |
| 3  | 255 | 217 | 186 | 159 | 137 | 118 | 102 | 87 | 76 | 66 | 53  | 25  | 11  | 5   | 2   | 1   |
| 4  | 255 | 216 | 183 | 155 | 131 | 111 | 95  | 79 | 67 | 57 | 48  | 42  | 35  | 29  | 24  | 21  |
| 5  | 255 | 219 | 189 | 163 | 141 | 122 | 107 | 90 | 87 | 31 | 11  | 3   | 3   | 2   | 1   | 1   |
| 6  | 255 | 218 | 187 | 160 | 138 | 119 | 103 | 87 | 72 | 45 | 18  | 6   | 5   | 3   | 2   | 2   |
| 7  | 255 | 217 | 184 | 157 | 133 | 113 | 96  | 78 | 67 | 53 | 34  | 17  | 6   | 5   | 4   | 3   |
| 8  | 255 | 222 | 192 | 167 | 146 | 128 | 114 | 87 | 78 | 63 | 40  | 9   | 8   | 6   | 4   | 3   |
| 9  | 255 | 217 | 184 | 157 | 135 | 115 | 99  | 84 | 73 | 65 | 56  | 48  | 18  | 11  | 6   | 2   |
| 10 | 255 | 219 | 189 | 163 | 141 | 122 | 107 | 90 | 74 | 40 | 15  | 5   | 4   | 3   | 2   | 1   |
| 11 | 255 | 214 | 180 | 151 | 127 | 108 | 91  | 76 | 65 | 56 | 47  | 41  | 35  | 31  | 27  | 24  |
| 12 | 255 | 215 | 181 | 152 | 129 | 109 | 93  | 78 | 67 | 57 | 49  | 43  | 38  | 33  | 29  | 27  |
| 13 | 255 | 218 | 187 | 160 | 138 | 119 | 102 | 87 | 75 | 56 | 34  | 19  | 7   | 4   | 2   | 2   |
| 14 | 255 | 219 | 188 | 162 | 139 | 120 | 103 | 80 | 69 | 34 | 12  | 3   | 3   | 2   | 1   | 1   |
| 15 | 255 | 219 | 189 | 164 | 143 | 124 | 108 | 69 | 20 | 5  | 0   | 1   | 1   | 1   | 1   | 0   |
| 16 | 255 | 217 | 185 | 158 | 136 | 117 | 101 | 86 | 76 | 67 | 58  | 47  | 15  | 11  | 7   | 6   |
| 17 | 255 | 217 | 184 | 157 | 135 | 115 | 99  | 84 | 74 | 63 | 54  | 47  | 16  | 10  | 7   | 5   |
| 18 | 255 | 213 | 178 | 149 | 124 | 104 | 87  | 72 | 60 | 50 | 42  | 35  | 29  | 25  | 21  | 18  |
| 19 | 255 | 215 | 181 | 152 | 127 | 105 | 86  | 58 | 46 | 21 | 10  | 2   | 0   | 0   | 0   | 0   |
| 20 | 255 | 214 | 179 | 149 | 125 | 104 | 87  | 72 | 61 | 51 | 43  | 36  | 31  | 27  | 23  | 20  |

Table 2: Scale values for latent

|         |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
|---------|----|----|----|----|----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--|
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| k       | Q0 | Q1 | Q2 | Q3 | Q4 | Q5 | Q6  | Q7  | Q8  | Q9  | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 0       | 1  | 1  | 0  | 0  | 0  | 1  | 1   | 2   | 3   | 12  | 27  | 44  | 178 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 1       | 0  | 0  | 7  | 17 | 29 | 45 | 70  | 107 | 160 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 2       | 10 | 13 | 16 | 20 | 24 | 29 | 35  | 41  | 53  | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 3       | 0  | 1  | 5  | 9  | 14 | 20 | 26  | 37  | 51  | 81  | 124 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 4       | 0  | 0  | 0  | 1  | 4  | 6  | 9   | 11  | 16  | 24  | 37  | 53  | 87  | 108 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 5       | 6  | 12 | 17 | 24 | 31 | 41 | 56  | 85  | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 6       | 11 | 15 | 18 | 22 | 27 | 33 | 41  | 48  | 53  | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 7       | 0  | 0  | 0  | 5  | 11 | 17 | 27  | 46  | 75  | 124 | 220 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 8       | 0  | 8  | 25 | 43 | 66 | 94 | 133 | 168 | 231 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 9       | 0  | 0  | 2  | 6  | 11 | 16 | 23  | 31  | 44  | 71  | 104 | 158 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 10      | 7  | 12 | 17 | 22 | 28 | 36 | 47  | 59  | 81  | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 11      | 0  | 0  | 0  | 1  | 2  | 4  | 5   | 7   | 9   | 12  | 15  | 19  | 23  | 27  | 30  | 38  |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 12      | 0  | 0  | 1  | 2  | 4  | 6  | 9   | 11  | 14  | 20  | 28  | 37  | 57  | 65  | 75  | 96  |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 13      | 0  | 3  | 7  | 11 | 16 | 21 | 28  | 39  | 54  | 67  | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 14      | 13 | 18 | 22 | 28 | 34 | 43 | 56  | 72  | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 15      | 0  | 0  | 4  | 13 | 23 | 37 | 56  | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 16      | 4  | 7  | 11 | 14 | 19 | 24 | 30  | 39  | 49  | 70  | 96  | 123 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 17      | 0  | 0  | 3  | 7  | 11 | 16 | 21  | 28  | 38  | 54  | 73  | 108 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 18      | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0   | 0   | 2   | 3   | 5   | 7   | 9   | 11  |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 19      | 5  | 12 | 18 | 26 | 34 | 43 | 56  | 84  | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |
| 20      | 0  | 0  | 0  | 0  | 0  | 0  | 1   | 2   | 3   | 5   | 8   | 11  | 14  | 16  | 18  | 21  |  |
| +=====+ |    |    |    |    |    |    |     |     |     |     |     |     |     |     |     |     |  |

Table 3: Dead zone values for latent

|    |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| k  | Q0  | Q1  | Q2  | Q3  | Q4  | Q5  | Q6  | Q7  | Q8  | Q9  | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |
| 0  | 233 | 228 | 222 | 214 | 204 | 191 | 176 | 155 | 135 | 106 | 66  | 32  | 0   | 0   | 0   | 0   |
| 1  | 94  | 85  | 72  | 59  | 45  | 32  | 21  | 10  | 4   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 2  | 91  | 75  | 58  | 43  | 29  | 17  | 9   | 4   | 2   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 3  | 112 | 96  | 81  | 65  | 51  | 38  | 26  | 16  | 10  | 4   | 1   | 0   | 0   | 0   | 0   | 0   |
| 4  | 149 | 138 | 125 | 109 | 93  | 77  | 61  | 45  | 32  | 21  | 12  | 7   | 3   | 1   | 0   | 0   |
| 5  | 65  | 50  | 36  | 24  | 14  | 8   | 4   | 2   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 6  | 92  | 75  | 59  | 43  | 29  | 18  | 10  | 5   | 2   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 7  | 118 | 107 | 97  | 74  | 60  | 48  | 38  | 29  | 17  | 6   | 0   | 0   | 0   | 0   | 0   | 0   |
| 8  | 55  | 47  | 36  | 27  | 19  | 13  | 8   | 3   | 2   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 9  | 122 | 107 | 92  | 76  | 60  | 46  | 34  | 22  | 15  | 9   | 4   | 2   | 0   | 0   | 0   | 0   |
| 10 | 82  | 67  | 53  | 40  | 29  | 20  | 14  | 8   | 4   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 11 | 190 | 181 | 171 | 160 | 149 | 135 | 120 | 101 | 85  | 68  | 52  | 38  | 26  | 17  | 10  | 6   |
| 12 | 175 | 165 | 154 | 143 | 128 | 113 | 98  | 81  | 67  | 53  | 41  | 31  | 23  | 15  | 9   | 5   |
| 13 | 100 | 85  | 70  | 56  | 42  | 31  | 21  | 12  | 6   | 1   | 0   | 0   | 0   | 0   | 0   | 0   |
| 14 | 80  | 64  | 49  | 35  | 23  | 14  | 7   | 2   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 15 | 62  | 47  | 33  | 21  | 12  | 6   | 3   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 16 | 125 | 109 | 92  | 75  | 59  | 43  | 30  | 18  | 10  | 5   | 1   | 1   | 0   | 0   | 0   | 0   |
| 17 | 130 | 114 | 98  | 82  | 66  | 50  | 37  | 24  | 15  | 7   | 2   | 1   | 0   | 0   | 0   | 0   |
| 18 | 236 | 233 | 229 | 224 | 219 | 213 | 206 | 198 | 189 | 180 | 169 | 158 | 146 | 132 | 118 | 104 |
| 19 | 90  | 72  | 54  | 37  | 24  | 15  | 9   | 3   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 20 | 219 | 213 | 207 | 199 | 190 | 181 | 172 | 160 | 148 | 133 | 118 | 103 | 88  | 74  | 62  | 51  |

Table 4: Decay (r) values for latent

|    |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| k  | Q0  | Q1  | Q2  | Q3  | Q4  | Q5  | Q6  | Q7  | Q8  | Q9  | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |
| 0  | 12  | 14  | 18  | 22  | 27  | 35  | 44  | 57  | 78  | 106 | 152 | 201 | 255 | 255 | 255 | 255 |
| 1  | 162 | 171 | 184 | 197 | 211 | 224 | 235 | 246 | 252 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 2  | 137 | 147 | 158 | 171 | 184 | 198 | 212 | 228 | 241 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 3  | 134 | 142 | 152 | 163 | 175 | 188 | 201 | 216 | 228 | 242 | 253 | 255 | 255 | 255 | 255 | 255 |
| 4  | 107 | 118 | 126 | 135 | 144 | 155 | 166 | 179 | 192 | 207 | 223 | 235 | 248 | 253 | 255 | 255 |
| 5  | 138 | 152 | 167 | 183 | 199 | 215 | 231 | 246 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 6  | 118 | 130 | 144 | 158 | 174 | 190 | 206 | 223 | 237 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 7  | 138 | 149 | 159 | 167 | 180 | 194 | 208 | 227 | 239 | 250 | 255 | 255 | 255 | 255 | 255 | 255 |
| 8  | 201 | 209 | 220 | 229 | 237 | 243 | 248 | 253 | 254 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 9  | 114 | 123 | 133 | 145 | 158 | 172 | 186 | 204 | 218 | 234 | 246 | 253 | 255 | 255 | 255 | 255 |
| 10 | 145 | 157 | 169 | 182 | 196 | 209 | 223 | 237 | 248 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 11 | 66  | 75  | 85  | 96  | 107 | 115 | 122 | 132 | 140 | 151 | 163 | 175 | 189 | 201 | 213 | 224 |
| 12 | 81  | 91  | 102 | 113 | 122 | 131 | 140 | 153 | 164 | 177 | 192 | 205 | 220 | 230 | 238 | 244 |
| 13 | 143 | 153 | 163 | 175 | 187 | 199 | 211 | 226 | 237 | 249 | 255 | 255 | 255 | 255 | 255 | 255 |
| 14 | 146 | 157 | 170 | 183 | 198 | 213 | 228 | 245 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 15 | 159 | 168 | 179 | 193 | 208 | 222 | 237 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 16 | 122 | 130 | 140 | 150 | 161 | 174 | 187 | 203 | 216 | 232 | 245 | 253 | 255 | 255 | 255 | 255 |
| 17 | 121 | 128 | 137 | 147 | 159 | 170 | 183 | 198 | 212 | 228 | 241 | 250 | 255 | 255 | 255 | 255 |
| 18 | 20  | 23  | 27  | 32  | 37  | 43  | 50  | 58  | 67  | 76  | 87  | 98  | 108 | 116 | 125 | 134 |
| 19 | 104 | 120 | 139 | 159 | 182 | 205 | 227 | 251 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 20 | 37  | 43  | 49  | 57  | 66  | 75  | 84  | 96  | 106 | 115 | 126 | 137 | 148 | 159 | 169 | 180 |

Table 5: P(0) values for latent

|    |     |     |     |     |     |     |     |    |    |    |     |     |     |     |     |     |
|----|-----|-----|-----|-----|-----|-----|-----|----|----|----|-----|-----|-----|-----|-----|-----|
| k  | Q0  | Q1  | Q2  | Q3  | Q4  | Q5  | Q6  | Q7 | Q8 | Q9 | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |
| 0  | 255 | 215 | 181 | 153 | 129 | 109 | 93  | 78 | 67 | 58 | 51  | 45  | 40  | 35  | 31  | 27  |
| 1  | 255 | 215 | 181 | 153 | 128 | 108 | 91  | 77 | 65 | 55 | 47  | 41  | 36  | 31  | 27  | 24  |
| 2  | 255 | 233 | 205 | 175 | 146 | 120 | 97  | 77 | 62 | 49 | 40  | 33  | 27  | 23  | 19  | 15  |
| 3  | 255 | 215 | 181 | 152 | 127 | 107 | 89  | 74 | 62 | 53 | 44  | 37  | 32  | 28  | 24  | 21  |
| 4  | 255 | 216 | 182 | 154 | 131 | 111 | 95  | 81 | 70 | 63 | 57  | 51  | 47  | 41  | 36  | 31  |
| 5  | 255 | 215 | 181 | 152 | 128 | 108 | 91  | 76 | 64 | 55 | 46  | 39  | 34  | 29  | 25  | 21  |
| 6  | 255 | 216 | 182 | 155 | 131 | 111 | 95  | 81 | 71 | 65 | 60  | 53  | 47  | 41  | 36  | 32  |
| 7  | 255 | 216 | 183 | 155 | 132 | 113 | 98  | 87 | 79 | 79 | 78  | 69  | 62  | 53  | 46  | 40  |
| 8  | 255 | 215 | 181 | 152 | 128 | 108 | 91  | 77 | 65 | 56 | 47  | 41  | 36  | 31  | 27  | 24  |
| 9  | 255 | 216 | 183 | 155 | 131 | 112 | 96  | 82 | 71 | 62 | 54  | 47  | 41  | 37  | 34  | 42  |
| 10 | 121 | 114 | 102 | 84  | 61  | 43  | 31  | 1  | 0  | 2  | 131 | 188 | 255 | 216 | 181 | 151 |
| 11 | 255 | 215 | 182 | 153 | 129 | 108 | 91  | 77 | 65 | 55 | 47  | 40  | 34  | 28  | 24  | 20  |
| 12 | 255 | 217 | 184 | 155 | 130 | 110 | 92  | 77 | 64 | 54 | 45  | 38  | 32  | 27  | 23  | 19  |
| 13 | 255 | 227 | 196 | 166 | 140 | 118 | 98  | 82 | 69 | 57 | 48  | 40  | 34  | 29  | 24  | 20  |
| 14 | 255 | 216 | 182 | 154 | 130 | 110 | 93  | 80 | 69 | 60 | 53  | 47  | 42  | 37  | 32  | 28  |
| 15 | 255 | 216 | 184 | 156 | 133 | 114 | 98  | 87 | 77 | 72 | 66  | 59  | 52  | 46  | 40  | 36  |
| 16 | 255 | 216 | 184 | 156 | 134 | 115 | 100 | 91 | 82 | 77 | 67  | 59  | 52  | 46  | 40  | 36  |
| 17 | 255 | 216 | 183 | 155 | 131 | 110 | 93  | 78 | 66 | 57 | 49  | 42  | 37  | 32  | 28  | 25  |
| 18 | 71  | 65  | 60  | 54  | 49  | 45  | 42  | 45 | 49 | 92 | 189 | 235 | 255 | 213 | 177 | 146 |

Table 6: Scale values for state

|    |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| k  | Q0  | Q1  | Q2  | Q3  | Q4  | Q5  | Q6  | Q7  | Q8  | Q9  | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |
| 0  | 13  | 12  | 11  | 11  | 11  | 11  | 11  | 11  | 11  | 13  | 12  | 9   | 7   | 13  | 19  | 26  |
| 1  | 16  | 14  | 12  | 11  | 9   | 8   | 7   | 4   | 4   | 4   | 4   | 5   | 7   | 5   | 3   | 7   |
| 2  | 9   | 8   | 7   | 6   | 6   | 4   | 3   | 3   | 2   | 3   | 2   | 0   | 3   | 2   | 4   | 4   |
| 3  | 6   | 8   | 8   | 9   | 9   | 9   | 10  | 8   | 8   | 11  | 11  | 10  | 15  | 22  | 28  | 37  |
| 4  | 20  | 18  | 17  | 16  | 15  | 15  | 15  | 14  | 13  | 14  | 13  | 9   | 9   | 14  | 21  | 30  |
| 5  | 10  | 8   | 7   | 5   | 4   | 4   | 3   | 3   | 2   | 3   | 4   | 6   | 8   | 9   | 10  | 10  |
| 6  | 13  | 13  | 13  | 13  | 13  | 13  | 14  | 12  | 12  | 11  | 2   | 1   | 10  | 17  | 24  | 34  |
| 7  | 35  | 30  | 25  | 22  | 19  | 17  | 16  | 18  | 15  | 22  | 0   | 1   | 0   | 4   | 7   | 12  |
| 8  | 13  | 11  | 9   | 8   | 6   | 5   | 4   | 3   | 2   | 3   | 3   | 4   | 9   | 6   | 2   | 5   |
| 9  | 15  | 15  | 15  | 15  | 15  | 16  | 17  | 17  | 18  | 16  | 20  | 26  | 34  | 46  | 75  | 255 |
| 10 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 2   | 0   | 0   | 0   | 0   | 0   | 0   |
| 11 | 9   | 7   | 6   | 5   | 4   | 3   | 2   | 1   | 1   | 0   | 0   | 1   | 2   | 2   | 3   | 3   |
| 12 | 11  | 9   | 6   | 5   | 3   | 2   | 2   | 2   | 2   | 3   | 4   | 4   | 3   | 3   | 3   | 2   |
| 13 | 10  | 8   | 6   | 5   | 4   | 3   | 2   | 2   | 1   | 2   | 2   | 2   | 4   | 3   | 4   | 1   |
| 14 | 23  | 19  | 17  | 14  | 12  | 11  | 9   | 8   | 8   | 11  | 9   | 4   | 4   | 7   | 9   | 13  |
| 15 | 14  | 14  | 14  | 15  | 16  | 17  | 18  | 20  | 18  | 0   | 8   | 13  | 14  | 23  | 33  | 50  |
| 16 | 26  | 24  | 21  | 19  | 17  | 16  | 12  | 7   | 0   | 11  | 14  | 14  | 17  | 24  | 32  | 46  |
| 17 | 43  | 38  | 32  | 27  | 22  | 18  | 14  | 7   | 1   | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 18 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 121 | 29  | 4   | 1   | 0   | 1   | 4   |

Table 7: Dead zone values for state



|  |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
|--|---|----------------------|----|----|----|----|----|----|----|-----------------------|-----|-----|-----|-----|-----|------------------------------|----|---|---|---|---|---|----|----|
| k  | Q0  | Q1                   | Q2 | Q3 | Q4 | Q5 | Q6 | Q7 | Q8 | Q9                    | Q10 | Q11 | Q12 | Q13 | Q14 | Q15                          |    |   |   |   |   |   |    |    |
| 0  | 207 199 190 181 169 158 145 130 116 103 90                      | 77 66 52 39 27       |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 1  | 224 218 212 205 196 187 177 165 152 139 126 112 101 87          |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 74 60                        |    |   |   |   |   |   |    |    |
| 2  | 253 253 252 252 251 250 249 247 245 242 239 235 231 226 220 213 |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 3  | 207 199 190 180 169 157 144 128 113 99                          |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 82 68 56 46 37 30            |    |   |   |   |   |   |    |    |
| 4  | 197 187 177 165 152 139 124 109 95                              | 84 74 64 56 42 30 19 |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 5  | 233 229 224 218 212 205 197 187 177 166 154 140 127 112 97      |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 81                           |    |   |   |   |   |   |    |    |
| 6  | 190 181 170 158 144 130 115 100 86                              | 78 70 60 48 36 25 16 |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 7  | 198 189 178 167 154 141 127 115 106 107 107 96                  |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 86 71 57 43                  |    |   |   |   |   |   |    |    |
| 8  | 232 227 223 217 210 203 194 183 173 161 149 136 124 111 99      | 84                   |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 9  | 180 168 156 143 128 112 97                                      |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 79 64 50 37 25 17 10 7 5     |    |   |   |   |   |   |    |    |
| 10 4   | 3   | 1                    | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 19 104 132 117 100 83 |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 11 245 243 240 237 234 230 226 220 214 208 200 191 182 171 160 147 |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 12 251 251 250 249 247 246 244 241 239 235 232 227 222 216 210 202 |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 13 254 253 253 253 252 251 250 249 248 246 244 242 239 236 233 229 |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 14 210 203 194 185 174 162 149 136 122 109 98                      |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 88 78 64 51 38               |    |   |   |   |   |   |    |    |
| 15 173 162 149 135 120 105 91                                      | 78 67 63 53 43 32 22 15 9                                       |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 16 169 156 142 128 112 98  |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 85 77 71 61 48 37 28 18 10 5 |    |   |   |   |   |   |    |    |
| 17 223 218 212 205 197 188 179 166 155 143 131 120 110 99          | 89 79   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     |                              |    |   |   |   |   |   |    |    |
| 18 22  |   |                      |    |    |    |    |    |    |    |                       |     |     |     |     |     | 17                           | 12 | 7 | 4 | 2 | 1 | 2 | 11 | 90 |

Table 8: Decay (r) values for state

|         |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|---------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| k       | Q0  | Q1  | Q2  | Q3  | Q4  | Q5  | Q6  | Q7  | Q8  | Q9  | Q10 | Q11 | Q12 | Q13 | Q14 | Q15 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 0       | 40  | 45  | 52  | 59  | 67  | 75  | 84  | 95  | 105 | 115 | 124 | 132 | 139 | 153 | 167 | 182 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 1       | 24  | 28  | 32  | 37  | 43  | 49  | 56  | 63  | 72  | 80  | 90  | 100 | 110 | 119 | 128 | 142 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 2       | 1   | 2   | 2   | 2   | 2   | 3   | 4   | 5   | 6   | 7   | 9   | 11  | 13  | 16  | 19  | 23  |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 3       | 35  | 41  | 48  | 56  | 65  | 75  | 85  | 97  | 109 | 124 | 139 | 153 | 168 | 183 | 197 | 210 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 4       | 45  | 50  | 56  | 64  | 72  | 81  | 90  | 101 | 110 | 118 | 125 | 132 | 139 | 155 | 171 | 188 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 5       | 15  | 18  | 21  | 24  | 29  | 33  | 39  | 45  | 52  | 60  | 69  | 78  | 88  | 98  | 108 | 119 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 6       | 47  | 54  | 62  | 70  | 79  | 89  | 99  | 110 | 119 | 126 | 127 | 136 | 150 | 167 | 183 | 200 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 7       | 44  | 49  | 54  | 60  | 67  | 74  | 82  | 90  | 95  | 97  | 91  | 99  | 107 | 121 | 135 | 151 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 8       | 15  | 17  | 20  | 23  | 27  | 31  | 35  | 40  | 46  | 53  | 61  | 70  | 78  | 88  | 96  | 109 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 9       | 58  | 65  | 73  | 82  | 92  | 102 | 112 | 125 | 136 | 146 | 160 | 176 | 193 | 209 | 226 | 251 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 10      | 252 | 253 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 189 | 93  | 72  | 83  | 96  | 110 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 11      | 7   | 8   | 9   | 11  | 13  | 15  | 18  | 21  | 24  | 29  | 33  | 39  | 46  | 53  | 60  | 69  |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 12      | 2   | 3   | 3   | 4   | 4   | 5   | 6   | 7   | 9   | 11  | 13  | 15  | 17  | 21  | 24  | 29  |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 13      | 1   | 1   | 1   | 2   | 2   | 2   | 3   | 4   | 4   | 5   | 6   | 7   | 8   | 10  | 12  | 14  |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 14      | 25  | 28  | 33  | 39  | 45  | 52  | 60  | 70  | 79  | 89  | 98  | 106 | 114 | 128 | 142 | 157 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 15      | 56  | 64  | 73  | 83  | 93  | 105 | 116 | 128 | 135 | 131 | 142 | 155 | 168 | 185 | 201 | 218 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 16      | 53  | 61  | 69  | 78  | 88  | 98  | 109 | 116 | 121 | 131 | 145 | 159 | 172 | 188 | 204 | 220 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 17      | 17  | 21  | 25  | 31  | 39  | 45  | 52  | 58  | 65  | 74  | 84  | 94  | 105 | 116 | 128 | 139 |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 18      | 230 | 235 | 240 | 246 | 250 | 252 | 254 | 251 | 235 | 129 | 50  | 39  | 36  | 43  | 51  | 60  |
| +=====+ |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |

Table 9: P(0) values for state

#### 2.2.4. Vocoder

A vocoder is needed to turn the acoustic features into actual speech to fill in the audio for any missing packets. Although the decoder is not normative, certain properties are needed for DRED to function adequately. First, the vocoder SHOULD be able to start synthesizing speech by continuing an existing waveform, reducing the artifacts caused at the beginning of a lost packet. If such property cannot be achieved, then the implementation SHOULD at least make an attempt to synchronize the phase of the synthesized speech with the last received speech, and attempt some form of blending, e.g. by splicing the signals in the LPC residual domain.

A second important property of the vocoder is to not rely on more than one feature vector of look-ahead. To synthesize speech between time  $t-10\text{ms}$  and  $t$ , the vocoder SHOULD NOT rely on acoustic features centered beyond  $t+5\text{ms}$  (i.e. covering  $t-5\text{ms}$  to  $t+15\text{ms}$ ). The vocoder MAY use more look-ahead when it is available, but there are cases (e.g. last lost packet) where the amount of acoustic feature vectors will be limited. For frames sizes less than 20 ms, the decoder SHOULD be prelated to deal with having less than one feature vector of look-ahead.

### 3. DRED Extension Format

We use the Opus extension mechanism [opus-extension] to add deep redundancy within the padding of an Opus packet. We use the extension ID 32, which means that the L flag signals whether a length code is included. In this document, we define only the extension payload. [Note: until adoption by the IETF, experimental implementations of DRED MUST use experiment extension ID 126 to avoid causing interoperability problems]

The principles behind the DRED mechanism defined in this extension are explained in [dred-paper]. All the data in the extension payload is encoded using the Opus entropy coder defined in Section 4.1 of [RFC6716]. Since some of the fields at the beginning of the payload are encoded with flat binary probabilities, they can still be interpreted as bits.

The extension starts with a 4-bit initial quantizer field ( $Q_0$ ) ranging from 0 to 15. That quantizer is used on the most recent frame encoded and is followed by the 3-bit quantizer slope  $dQ$ . The 3-bit  $dQ$  index selects from the following values: [0, 1/8, 3/16, 1/4, 3/8, 1/2, 3/4, 1] quantizer step per frame. The quantizer for frame  $k$  is thus given by:  $q = \min(Q_{\max}, \text{round}(Q_0 + dQ\_table[dQ] * k))$ , where  $Q_{\max}$  is the maximum quantizer allowed. For example, using  $Q_0=5$  and  $dQ=2$  (3/16), frame  $k=20$  would use a quantizer of  $\text{round}(5 + 3/16 * k) = 9$ .

We then have one bit ( $X$ ) that flags whether an extended offset is used. If  $X=0$ , then a 5-bit offset indicator follows. The offset is a positive integer in units of 2.5 ms. It indicates the time of the last sample analysed for the transmitted features in the packet, measured from 40ms after the first sample in the Opus frame that contains the extension data.

If  $X=1$ , then we have an extended offset field, with an additional 8 bits to signal the offset. This makes it possible to signal a maximum offset of  $(2^{13}-1)*2.5\text{ms}$ , or approximately 20.5 seconds.

If  $Q_0 < 14$  and  $dQ \neq 0$ , then the offset is followed by the range-coded  $Q_{\max}$  parameter. The probability of  $Q_{\max}=15$  is set to 1/2 (one bit is used), whereas other possible values ( $Q_0 < Q_{\max} < 15$ ) are coded with a flat probability distribution. The pdf for  $Q_{\max}$  is  $\{nval, 1, 1, \dots\} / (2*nval)$ , where there are  $nval=14-Q_0$  ones. The  $Q_{\max}=15$  symbol is first, followed by other values in ascending order, starting from  $Q_{\max}=Q_0+1$ .

The compressed redundancy information consists of an initial state coded, followed by a sequence of 40-ms latent vectors. Both the initial state and the latent vectors are entropy-coded using a Laplace distribution. The number of 40-ms DRED latent vectors is not coded explicitly. Instead, the decoder keeps decoding them until it runs out of bits. More specifically, the decoder MUST NOT decode blocks when fewer than 8 bits remain in the DRED payload. There is no arbitrary limit on the number of vectors that can be coded in a packet, but the authors do not believe that using more than a few seconds of redundancy is likely to be useful. Also, decoders MAY ignore any redundancy data beyond a certain amount.

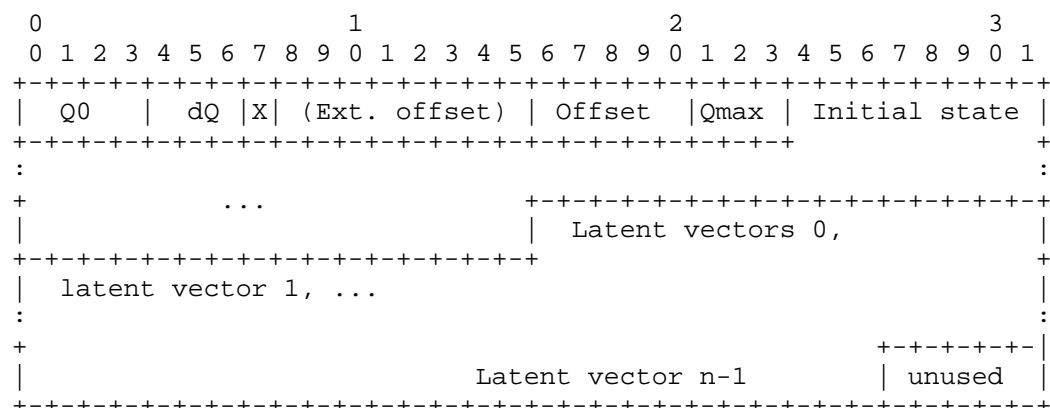


Figure 3: Extension framing

### 3.1. Latent decoding

Since the DRED decoder is normative, we describe DRED from the decoder perspective, but the encoder is expected to have the corresponding behavior. DRED uses the same range coder as the rest of Opus, as described in Section 4.1 of [RFC6716]. Because the non-entropy-coded bits (Q0, dQ, ...) do not amount to an integer number of bytes, it is simpler to code them using the range coder. The result is the same for those bits, but it ensures that the complete DRED payload is an integer number of bytes (which is important to handle the end condition).

The initial state and latent vectors are handled in the same way, both coded one dimension at a time. For each dimension, the decoder uses the quantization tables to determine the `_r_` and `_p0_` parameters. If `r=0` or `p0=255` for the current symbols and quantizer, then no symbol is decoded and the decoded quantized value is 0. Otherwise, decoding proceeds as follows.

The first symbol decoded determines whether the quantized index is zero, positive, or negative (in that order). The decoder uses the pdf  $\{2 \cdot p0_{\{i,q\}}, 256 - p0_{\{i,q\}}, 256 - p0_{\{i,q\}}\} / 512$ . If the value is non-zero, a second symbol is decoded. We start by generating an "inverse cdf" in Q15:

$$\text{icdf}(i) = \begin{cases} / 32768 & , \text{ if } i < 0 \\ \text{MAX}(7, 128 * r_{\{i,q\}}) & , \text{ if } i = 0 \\ \text{MAX}(7-i, (\text{icdf}[i-1] * r_{\{i,q\}}) // 32768) & , \text{ if } 0 < i < 7 \\ 0 & , \text{ if } i \geq 7 \end{cases}$$

where // denotes the truncating integer division. The pdf is then given by  $\text{pdf}[i] = \text{icdf}[i-1] - \text{icdf}[i]$ . If the decoded symbol equals 7, then another symbol is decoded and added to the 7 already decoded. The process is repeated until the decoded symbol is different from 7. At that point, the sign is applied and the decoded value is equal to  $\text{quantized\_index} * 256 / s_{\{i,q\}}$ .

#### 4. Conformance

As for the Opus specification, we wish to allow the greatest possible choice of freedom in implementing the DRED specification. For that reason, conformance is defined through the DRED decoder only. The two decoder components -- the feature decoder and vocoder -- are handled separately, and differently from each other.

##### 4.1. DRED Feature Decoding

DRED acoustic feature decoding is strictly defined. The decoder implementation MUST use the same weights provided in this specification. The DNN weights can be further quantized and the exact implementation of the DNN arithmetic (including activation functions) can be approximated, provided that they comply with the following test. An alternate DNN model is not allowed, as it would be easy to overfit a model to the test.

##### 4.2. Vocoder

While the vocoder that synthesizes the audio from the decoded acoustic features isn't normative, defining how the vocoder behaves helps defining the meaning of the features themselves.

We provide a set of test vectors where the input file contains acoustic features and the corresponding original audio from which the features were computed. To verify an vocoder implementation, we will provide a tool [TBD] that compares the vocoder output to the reference output. The comparison thresholds are meant to accept any vocoder that sounds sufficiently similar. Also, no waveform-domain comparison is possible since the acoustic features do not capture phase information.

The test vector material MUST NOT be used to train the vocoder since there would be a risk of overfitting.

## 5. IANA Considerations

[Note: Until the IANA performs the actions described below, implementers should use 126 instead of 32 as the extension number. Moreover, the DRED payload temporarily uses a two-byte prefix for compatibility: a 'D' character, followed by a version number (currently 10).]

This document assigns ID 32 to the "Opus Extension IDs" registry created in [opus-extension] to implement the proposed DRED extension.

### 5.1. Opus Media Type Update

This document updates the audio/opus media type registration [RFC7587] to add the following two optional parameters:

ext32-dred-duration: Specifies the maximum amount of DRED information (in milliseconds) that the receiver can use. The receiver MUST be able to handle any valid DRED duration even if it does not make use of it. The sender MUST NOT send more than the specified amount of redundancy to avoid leaking information beyond what the receiver expects.

sprop-ext32-dred-duration: Maximum amount of DRED information (in milliseconds) that the sender is likely to use. The receiver MUST be able to handle any valid DRED duration even if it does not make use of it. The sender MUST NOT send more than the specified amount of redundancy to avoid leaking information beyond what the receiver expects.

### 5.2. Mapping to SDP Parameters

The media type parameters described above map to declarative SDP and SDP offer-answer in the same way as other optional parameters in [RFC7587]. Regardless of any a=fmtp SDP attribute specified, the receiver MUST be capable of receiving any signal.

## 6. Security Considerations

When using a Selective Forwarding Unit (SFU), it is possible for the DRED payload to include speech that would not otherwise have been transmitted. For example, a new user joining may receive audio that was transmitted before them joining. If such behavior is a security or confidentiality concern, then the SFU SHOULD use the ext32-dred-duration and sprop-ext32-dred-duration parameters to limit the amount

of redundancy and/or temporarily drop DRED payloads when that could leak information.

As is the case for any media codec, the decoder must be robust against malicious payloads. Similarly, the encoder must also be robust to malicious audio input since the encoder input can often be controlled by an attacker. That can happen through browser JS, echo, or when the encoder is on a gateway.

DRED is designed to have a complexity that is independent of the signal characteristics. However, there exist implementation details that can cause signal-dependent complexity changes. One example is CPU treatment of denormals that can sometimes cause increased CPU load and could be triggered by malicious input. For that reason, it is important to minimize such impact to reduce the impact of DOS attacks. Similarly, since the encoding and decoding process can be computationally costly, devices must manage the complexity to avoid attacks that could trigger too much DRED encoding or decoding to be performed.

The use of variable-bitrate (VBR) encoding in DRED poses a theoretical information leak threat [RFC6562], but that threat is believed to be significantly lower than that posed by VBR encoding in the main Opus payload. Since this document provides a way to dynamically vary the amount of redundancy transmitted, it is also possible to reduce the overall VBR risk of Opus by using DRED as a way of making the total Opus payload constant (CBR) or nearly constant.

## 7. References

### 7.1. Normative References

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- [RFC7587] Spittka, J., Vos, K., and JM. Valin, "RTP Payload Format for the Opus Speech and Audio Codec", RFC 7587, DOI 10.17487/RFC7587, June 2015, <<https://www.rfc-editor.org/info/rfc7587>>.
- [RFC8174] Leiba, B., "Ambiguity of Uppercase vs Lowercase in RFC 2119 Key Words", BCP 14, RFC 8174, DOI 10.17487/RFC8174, May 2017, <<https://www.rfc-editor.org/info/rfc8174>>.



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[opus-extension]

Terriberry, T.B. and J.-M. Valin, "Extension Formatting for the Opus Codec (draft-ietf-mlcodec-opus-extension)", October 2023.

## 7.2. Informative References

[RFC6562] Perkins, C. and JM. Valin, "Guidelines for the Use of Variable Bit Rate Audio with Secure RTP", RFC 6562, DOI 10.17487/RFC6562, March 2012, <<https://www.rfc-editor.org/info/rfc6562>>.

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